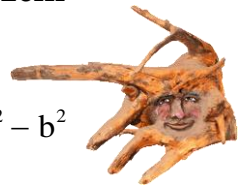


# Mathematik \* Jahrgangsstufe 9 \* Binomische Formeln und Wurzeln

Die drei binomischen Formeln lauten:

$$(a + b)^2 = a^2 + 2ab + b^2 \quad ; \quad (a - b)^2 = a^2 - 2ab + b^2 \quad ; \quad (a + b) \cdot (a - b) = a^2 - b^2$$



1. Ergänze so, dass man den Term als Produkt schreiben kann.

a)  $\frac{1}{4}x^2 + \square + 4 = (\quad)^2$       b)  $9a^2 - 24ab + \square = (\quad)^2$   
c)  $2,25x^2 + \square + \frac{1}{4} = (\quad)^2$       d)  $1,96a^2 - 14ab + \square = (\quad)^2$   
e)  $2x^2 + \square + 4 = (\quad)^2$       f)  $3a^2 - 2\sqrt{6}ab + \square = (\quad)^2$

2. Schreibe – falls möglich – den Term ohne Wurzel.

a)  $\sqrt{4x^2 + 2xy + 0,25y^2}$       b)  $\sqrt{36x^2 + 4y^2 - 24xy}$   
b)  $\sqrt{\frac{1}{4}x^2 + y^2 - xy}$       c)  $\sqrt{4 - 6a + 2,25a^2}$   
e)  $\sqrt{9x^2 + 18xy + 4y^2}$       f)  $\sqrt{9x^2 - 9x + 2,25}$



3. Vereinfache.

a)  $\frac{\sqrt{2}}{1 - \sqrt{2}}$       b)  $\frac{\sqrt{2}}{\sqrt{3}} + \frac{1}{\sqrt{6}}$       c)  $\frac{\sqrt{6}}{\sqrt{3} + \sqrt{2}}$   
d)  $\frac{\sqrt{2x^2 - 8}}{\sqrt{x + 2}}$       e)  $\frac{\sqrt{4xy}}{\sqrt{x} - \sqrt{y}}$       f)  $\frac{\sqrt{8x}}{\sqrt{2x} - 2}$

4. Vereinfache so weit wie möglich.

a)  $\sqrt{3x^2 - 12xy + 12y^2}$       b)  $\sqrt{0,5x^2 + 4,5y^2 - 3xy}$   
c)  $\sqrt{\frac{x^2 - 4x + 4}{4x - 8}}$       d)  $\frac{0,25a^2 + ab + b^2}{4a + 8b}$   
e)  $\frac{1}{\sqrt{2}} - \frac{2}{\sqrt{5}}$       f)  $\frac{3 + \sqrt{3}x + 0,25x^2}{x + 2\sqrt{3}}$



## Mathematik \* Jahrgangsstufe 9 \* Binomische Formeln und Wurzeln Lösungen

1. a)  $\frac{1}{4}x^2 + \boxed{2x} + 4 = \left(\frac{1}{2}x + 2\right)^2$     b)  $9a^2 - 24ab + \boxed{16b^2} = (3a - 4b)^2$   
 c)  $2,25x^2 + \boxed{1,5x} + \frac{1}{4} = \left(1,5x + \frac{1}{2}\right)^2$     d)  $1,96a^2 - 14ab + \boxed{25b^2} = (1,4a - 5b)^2$   
 e)  $2x^2 + \boxed{4\sqrt{2}x} + 4 = (\sqrt{2}x + 2)^2$     f)  $3a^2 - 2\sqrt{6}ab + \boxed{2b^2} = (\sqrt{3}a - \sqrt{2}b)^2$

2. a)  $\sqrt{4x^2 + 2xy + 0,25y^2} = \sqrt{(2x + 0,5y)^2} = |2x + 0,5y|$

b)  $\sqrt{36x^2 + 4y^2 - 24xy} = \sqrt{(6x - 2y)^2} = |6x - 2y|$

b)  $\sqrt{\frac{1}{4}x^2 + y^2 - xy} = \sqrt{\left(\frac{1}{2}x - y\right)^2} = \left|\frac{1}{2}x - y\right|$

c)  $\sqrt{4 - 6a + 2,25a^2} = \sqrt{(1,5a - 2)^2} = |1,5a - 2|$

e)  $\sqrt{9x^2 + 18xy + 4y^2}$  lässt sich nicht ohne Wurzel schreiben!

f)  $\sqrt{9x^2 - 9x + 2,25} = \sqrt{(3x - 1,5)^2} = |3x - 1,5|$



2. a)  $\frac{\sqrt{2}}{1 - \sqrt{2}} = \frac{\sqrt{2} \cdot (1 + \sqrt{2})}{(1 - \sqrt{2}) \cdot (1 + \sqrt{2})} = \frac{\sqrt{2} + 2}{1 - 2} = -2 - \sqrt{2}$

b)  $\frac{\sqrt{2}}{\sqrt{3}} + \frac{1}{\sqrt{6}} = \frac{\sqrt{2} \cdot \sqrt{6} + \sqrt{3}}{\sqrt{3} \cdot \sqrt{6}} = \frac{2 \cdot \sqrt{3} + \sqrt{3}}{3 \cdot \sqrt{2}} = \frac{3 \cdot \sqrt{3}}{3 \cdot \sqrt{2}} = \frac{\sqrt{3} \cdot \sqrt{2}}{\sqrt{2} \cdot \sqrt{2}} = \frac{\sqrt{6}}{2}$

c)  $\frac{\sqrt{6}}{\sqrt{3} + \sqrt{2}} = \frac{\sqrt{6} \cdot (\sqrt{3} - \sqrt{2})}{(\sqrt{3} + \sqrt{2}) \cdot (\sqrt{3} - \sqrt{2})} = \frac{3\sqrt{2} - 2\sqrt{3}}{3 - 2} = 3\sqrt{2} - 2\sqrt{3}$

d)  $\frac{\sqrt{2x^2 - 8}}{\sqrt{x + 2}} = \frac{\sqrt{2(x^2 - 4) \cdot (x + 2)}}{\sqrt{x + 2} \cdot \sqrt{x + 2}} = \frac{\sqrt{2(x - 2) \cdot (x + 2) \cdot (x + 2)}}{|x + 2|} = \sqrt{2(x - 2)}$

e)  $\frac{\sqrt{4xy}}{\sqrt{x} - \sqrt{y}} = \frac{\sqrt{4xy} \cdot (\sqrt{x} + \sqrt{y})}{(\sqrt{x} - \sqrt{y}) \cdot (\sqrt{x} + \sqrt{y})} = \frac{2x\sqrt{y} + 2y\sqrt{x}}{x - y}$

f)  $\frac{\sqrt{8x}}{\sqrt{2x} - 2} = \frac{2\sqrt{2x} \cdot (\sqrt{2x} + 2)}{(\sqrt{2x} - 2) \cdot (\sqrt{2x} + 2)} = \frac{4x + 4\sqrt{2x}}{2x - 4} = \frac{2x + 2\sqrt{2x}}{x - 2}$

$$4. a) \quad \sqrt{3x^2 - 12xy + 12y^2} = \sqrt{3 \cdot (x^2 - 4xy + 4y^2)} = \sqrt{3 \cdot (x-2y)^2} = |x-2y| \cdot \sqrt{3}$$

$$b) \quad \sqrt{0,5x^2 + 4,5y^2 - 3xy} = \sqrt{0,5 \cdot (x^2 - 6xy + 9y^2)} = \sqrt{\frac{2 \cdot (x-3y)^2}{4}} = \frac{|x-3y| \cdot \sqrt{2}}{2}$$

$$c) \quad \sqrt{\frac{x^2 - 4x + 4}{4x - 8}} = \sqrt{\frac{(x-2)^2}{4(x-2)}} = \sqrt{\frac{(x-2)}{4}} = \frac{\sqrt{x-2}}{2}$$

$$d) \quad \frac{0,25a^2 + ab + b^2}{4a + 8b} = \frac{0,25 \cdot (a^2 + 4ab + 4b^2)}{4 \cdot (a+2b)} = \frac{0,25 \cdot (a+2b)^2}{4 \cdot (a+2b)} = \frac{a+2b}{16}$$

$$e) \quad \frac{1}{\sqrt{2}} - \frac{2}{\sqrt{5}} = \frac{\sqrt{2}}{2} - \frac{2 \cdot \sqrt{5}}{5} = \frac{5\sqrt{2} - 4\sqrt{5}}{10} = 0,5\sqrt{2} - 0,4\sqrt{5}$$

$$f) \quad \frac{3 + \sqrt{3}x + 0,25x^2}{x + 2\sqrt{3}} = \frac{(\sqrt{3} + 0,5x)^2}{2 \cdot (0,5x + \sqrt{3})} = \frac{1}{2} \cdot (\sqrt{3} + 0,5x)$$

